

University of Turkish Aeronautical Association Aeronautics and Astronautics AEE 361-Applied Elasticity Midterm Examination – 25.11.2020, 06:40 p.m. Time allowed: 110 min.

• This is an open notes examination.

• You can use calculators without programming and graphical capabilities.

• Your solution must be neat and consistent, and must include all intermediate steps even if you think it is obvious.

Student ID:	
Name & Surname:	Signature

1. (10 *points*) Simplify (expand) the following expressions.  $\delta$  is Kronecker delta. In your final answer no letter indices must appear. (parts (a) and (b): each 3 *points*, part (c): 4 *points*)

(a)  $\delta_{kl}\delta_{lk}$ 

- (b)  $\delta_{jj}\delta_{kk}$
- (c)  $a_k b_m \delta_{ii} \delta_{km}$

2. (35 points) The state of stress at a point in a loaded solid is given as

$$\begin{bmatrix} \sigma \end{bmatrix} = \begin{bmatrix} 5 & 0 & 2 \\ 0 & 0 & 0 \\ 2 & 0 & -5 \end{bmatrix} MPa$$

(a) Calculate the principal stresses

(b) Plot the Mohr's circles for this point and calculate the maximum shear stress

(c) Determine the principal directions <u>only</u> for the largest principal stress.

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3. (30 *points*) The tensorial strain at a particular point in a loaded medium is found to be as follows:

$$\begin{bmatrix} \varepsilon \end{bmatrix} = \begin{bmatrix} 1 & -2 & 0 \\ -2 & 6 & 0 \\ 0 & 0 & 1 \end{bmatrix} \times 10^{-4}$$

(a) Calculate the normal strain at this point in the direction of the vector  $\vec{A} = \vec{e_1} + 2\vec{e_2} - 2\vec{e_3}$ (Hint: The direction cosines in this direction are the components of unit vector along vector  $\vec{A}$ )

(b) Considering a CCW rotation of 90° about the  $x_2$  - axis, construct the transformation matrix.

4. (25 points) A displacement field in a body is given by

$$u = c(x^{2} + 10)$$
$$v = 2cyz$$
$$w = c(-xy + z^{2})$$

where  $c = 10^{-4}$ . Determine the state of strain and stress on an element positioned at (0, 2, 1). Use E = 70 GPa and v = 0.3.